



SCATTERING PROPERTIES OF E. M. WAVES IN A MULTILAYERED CYLINDER FILLED WITH DOUBLE NEGATIVE AND POSITIVE MATERIALS

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ABSTRACT:

The meta-reinforcement cylinders have several layers. The patented expansion method in each region produces common formulas for electromagnetic fields. The picture property can be observed in a line source with a cylinder radius much larger than the wavelength. The distributions of the electromagnetic fields are shown if the line source is located near the two-façade cylinder alternately filled with double negative and double positive contents. The electrical field and energy with very little radius were investigated in the presence of a cylinder.

KEY-WORDS: E. M. Waves, Multilayered Cylinder, Double negative and positive, DNG.

INTRODUCTION:

In 1968 Veselago studied theoretically the characteristics of the waves in a particular medium, both of which are negatively permittivity and permeable. Hypothesis materials are systematically studied once the structure of the Split Ring Resonator [SRR] has been proposed and experimentally checked. Double negative (DNG) content has many optical characteristics and may lead to a perfect lens. Kong formulated wave reflections or refractions for EM waves which spread through a stratified DNG medium. The purpose of this paper is to extend the currents from planar to cylindrical structures in order to better understand metamaterials hybrid effects and cylindrical curvatures.

FORMULATIONS:

Consider an endlessly big N -layered cylinder (ϵ_0, μ_0) , as Figure 1 demonstrates. Per layer is filled with a DNG or DPS uniform material with varying permittivity and permeability. In the following analysis, the time dependence, $e^{-j\omega t}$, to the full is abolished. The admissibility and permeability of the substance in the region $f (f = 0, \dots, N)$ is as following:

$$\epsilon_f = u |\epsilon_f| \quad (1)$$

$$\mu_f = u |\mu_f|, \quad (2)$$

Where;

$$u = \begin{cases} -1, & \text{DNG material} \\ 1, & \text{DPS material.} \end{cases} \quad (3)$$

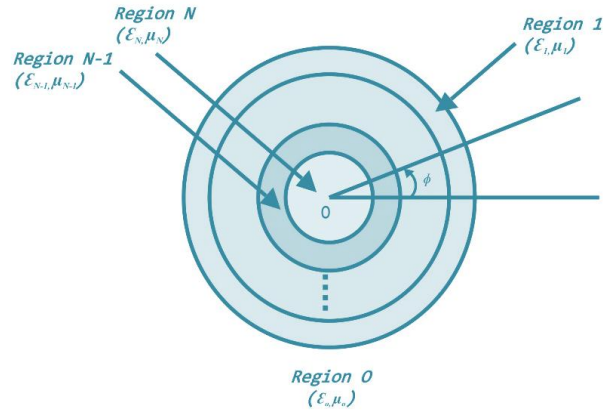


Figure 1: Multi-layer cylindrical geometry of different materials.

The layered cylinders would be illuminated at an arbitrary angles by an incident wave of transverse electric (TE) or transverse magnetic (TM).

$$\mathbf{M}_n^{(p)}(k_z) = \left[\hat{\rho} \frac{jn}{\rho} B_n^{(p)}(k_\rho \rho) - \hat{\phi} \frac{dB_n^{(p)}(k_\rho \rho)}{d\rho} \right] e^{j(n\phi + k_z z)} \quad (4)$$

$$\mathbf{N}_n^{(p)}(k_z) = \frac{1}{k} \left[\hat{\rho} j k_z \frac{dB_n^{(p)}(k_\rho \rho)}{d\rho} - \hat{\phi} \frac{nk_z}{\rho} B_n^{(p)}(k_\rho \rho) + \hat{z} k_\rho^2 B_n^{(p)}(k_\rho \rho) \right] e^{j(n\phi + k_z z)}, \quad (5)$$

The super scribble p is 1 & 3, representing the Hankel function of the first-type bessel and first-type cylinder and $k^2 = k_\rho^2 + k_z^2$, where the cylindrical verbessels n function is defined by $B_n^{(p)}(k_\rho \rho)$

$$\mathbf{M}_n^{(p)}(k) = \left[\hat{\rho} \frac{jn}{\rho} B_n^{(p)}(k\rho) - \hat{\phi} \frac{dB_n^{(p)}(k\rho)}{d\rho} \right] e^{jn\phi} \quad (6)$$

$$\mathbf{N}_n^{(p)}(k) = \hat{z} k B_n^{(p)}(k\rho) e^{jn\phi}. \quad (7)$$

The region's electromagnetic areas f are Represented as follows via the personality-function expansion method ($f = 1, \dots, N - 1$).

$$\begin{aligned} \mathbf{E}_f &= \sum_{n=0}^{\infty} \left\{ a_{nf} \mathbf{N}_n^{(3)}(k_{zf}) + b_{nf} \mathbf{M}_n^{(3)}(k_{zf}) + a'_{nf} \mathbf{N}_n^{(1)}(k_{zf}) \right. \\ &\quad \left. + b'_{nf} \mathbf{M}_n^{(1)}(k_{zf}) \right\} \end{aligned} \quad (8)$$

$$\begin{aligned} \mathbf{H}_f &= \frac{k_f}{j\omega |\mu_f|} \sum_{n=0}^{\infty} \left\{ a_{nf} \mathbf{M}_n^{(3)}(k_{zf}) + b_{nf} \mathbf{N}_n^{(3)}(k_{zf}) + a'_{nf} \mathbf{M}_n^{(1)}(k_{zf}) \right. \\ &\quad \left. + b'_{nf} \mathbf{N}_n^{(1)}(k_{zf}) \right\}, \end{aligned} \quad (9)$$

The unidentified extension variables are a_{nf} , b_{nf} , a'_{nf} and b'_{nf} .

In the outer layer area (i.e. area 0) and inner layer area (i.e. area N), the electromagnetic fields can be applied.

$$\begin{aligned} \mathbf{E}_0 &= \mathbf{E}^i + \mathbf{E}^s \\ &= \mathbf{E}^i + \sum_{n=0}^{\infty} \left[a_{n0} \mathbf{N}_n^{(3)}(k_{z0}) + b_{n0} \mathbf{M}_n^{(3)}(k_{z0}) \right] \end{aligned} \quad (10)$$

$$\begin{aligned} \mathbf{H}_0 &= \mathbf{H}^i + \mathbf{H}^s \\ &= \mathbf{H}^i + \frac{k_{z0}}{j\omega u |\mu_0|} \times \sum_{n=0}^{\infty} \left[a_{n0} \mathbf{M}_n^{(3)}(k_{z0}) + b_{n0} \mathbf{N}_n^{(3)}(k_{z0}) \right] \end{aligned} \quad (11)$$

And

$$\mathbf{E}_N = \sum_{n=0}^{\infty} \left[a'_{nN} \mathbf{N}_n^{(1)}(k_{zN}) + b'_{nN} \mathbf{M}_n^{(1)}(k_{zN}) \right] \quad (12)$$

$$\mathbf{H}_N = \frac{k_{zN}}{j\omega u |\mu_N|} \sum_{n=0}^{\infty} \left[a'_{nN} \mathbf{M}_n^{(1)}(k_{zN}) + b'_{nN} \mathbf{N}_n^{(1)}(k_{zN}) \right]. \quad (13)$$

Apply the measuring to cylindrical interfaces of the tangential electric or magnetic various strategies in the following formulas, a_{nf} , b_{nf} , a'_{nf} , and b'_{nf} , in $\rho = r_f$ (where $f = 0, 1, \dots, N - 1$):

$$\hat{\rho} \times \begin{bmatrix} \mathbf{E}_f \\ \mathbf{H}_f \end{bmatrix} = \hat{\rho} \times \begin{bmatrix} \mathbf{E}_{f+1} \\ \mathbf{H}_{f+1} \end{bmatrix}. \quad (14)$$

Finally, for parameters [Li *et al.*, 2000], a recursive approach can be used:

$$\mathbf{C}_{f+1} = \mathbf{T}_f \mathbf{C}_f, \quad (15)$$

So, where's the meaning of $[\mathbf{C}_f]$

$$\mathbf{C}_f = \left[a_{nf}, b_{nf}, a'_{nf}, b'_{nf} \right]^T, \quad (16)$$

The transmitter vector is defined in the own development domains

$$\mathbf{T}_f = \mathbf{F}_{f+1}^{-1} \mathbf{F}_f, \quad (17)$$

Two parameters arise from the variable matrices \mathbf{F}_f and \mathbf{F}_{f+1}

RESULT:

The length dispersion pattern of the two-layered cylinder (three areas) with various DPS components is determined to verify the correctness of these formulations, clarified by TE and TM waves and ray-coated, each with a separate line source.

Figure 2. Geometry screens. There are two layers $a = 0.25\lambda$ from the inside to the outside and $b = 0.3\lambda$. This, compressibility is oscillating to oscillating $\epsilon_{r1} = 4.0$ and to oscillating to oscillating to

oscillate $\epsilon_{r2} = 1.0$. There is a $\mu_{r1} = \mu_{r2} = 1.0$ connexion between two layers. The aircraft's waves shall usually occur.

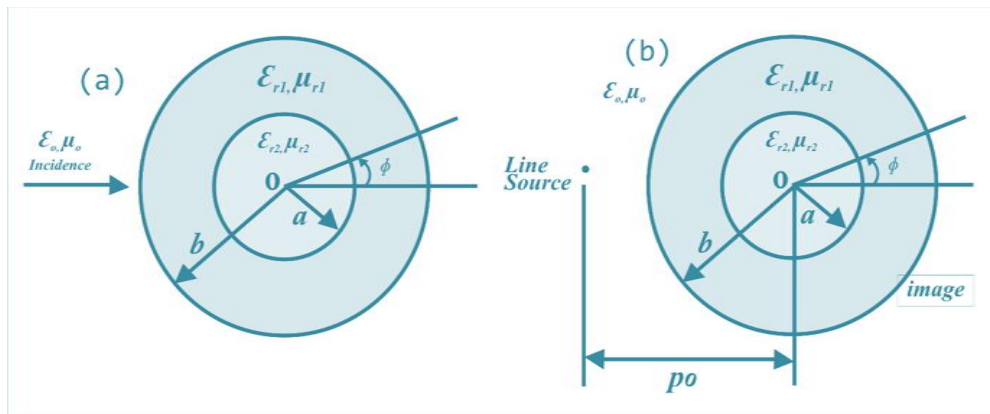


Figure: 2 Geometry of a two-layered cylindrical DPS-material.

CONCLUSION:

We utilize the autonomous extraction technique throughout this report to usually express areas in a double-negative and double-positive cylinder. The individual expansion coefficients are determined by continuous application of the electro-magnetic various strategies at their implementations. When a radius $r\lambda$ is found, a line source is shown with this cylinders. DNG and DPS-based materials were tested in the electric field and power of these small radii-filled cylinders.

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