



## STUDIES ON SEMICONDUCTOR WAVEGUIDE-CAVITY SYSTEM CONTAINING A SINGLE QUANTUM DOT

Pankaj Kumar<sup>1</sup> and Dr. Pramendra Ranjan Singh<sup>2</sup>

<sup>1</sup>Research Scholar, (In The Faculty Of Science, Physics) J. P. Univ Chapra .

<sup>2</sup>Principal , Narayan College, Goreyakothei (Siwan).

### ABSTRACT:

This paper presents the coherent light propagation effects in various semiconductor systems, including planar photonic crystals and micropillars.

**KEYWORDS:** Photonic crystals, Coherent light & Quantum dot

### INTRODUCTION :

The ability to couple waveguides and cavities offers exciting opportunities for integrated quantum optical devices using solids.[1-3] In particular, planar photonic crystals offer a technology platform, where quantum bits (qubits) can be manipulated from quantum dots (QDs) placed on field antinode positions within the cavity or waveguide.[4-6] Integrated semiconductor micropillar systems also show great promise for quantum optical applications [7-9]

### METHODOLOGY

We want to describe light propagation for QD- cavity geometry, where the input and output fields are identified separately from the cavity region, in which QD is assumed as embedded. An example

waveguide-cavity system is shown schematically in Fig. 1.(a,b,c) For a continuous wave (cw) waveguide mode of a photonic crystal system [10, 23]

$$r_{pc}(\omega) = \frac{i\omega\Gamma_c}{\omega_c^2 - \omega^2 - i\omega(\Gamma_c + \Gamma_0) - \omega\Sigma(\omega)} \quad (1)$$

where the self-energy is  $\omega(\omega) = \omega g^2 / (\omega_x - \omega^2 - i\omega\gamma_q)$ ,  $\Gamma_0 \equiv 2\kappa$   $\Gamma_0$  is the cavity decay rate through vertical scattering (unloaded cavity broadening),  $\gamma_f \equiv 2\kappa_c = 2(\kappa_l + \kappa_r)$  is the cavity-waveguide coupling rate coincides with the vacuum Rabi splitting which can be observed in transmission or reflection; this normal mode doublet can occur even if the dot is not in the strong-coupling regime,

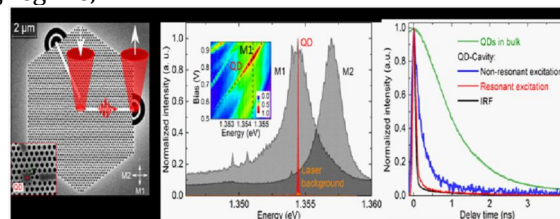
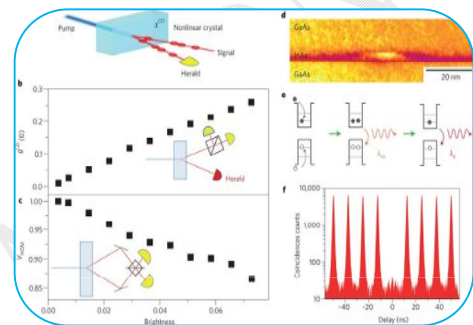


Fig -1 SEM image of the waveguide-coupled QD PhCC system



we will use a ME approach where exciton -photon interactions are easily included in all orders. Referring to Fig. 1 (a,b,c), we relate the left / right output operators to the cavity mode operator[24-27]

$$\langle a_{out}^r(t) \rangle = -\langle a_{in}(t) \rangle + \sqrt{2k_c} \langle a(t) \rangle, \tag{2}$$

$$\langle a_{out}^l(t) \rangle = \sqrt{2k_c} \langle a(t) \rangle \tag{3}$$

where, for a coherent cw input state,  $\langle a_{in} \rangle = i\eta_c / (2\sqrt{2k_c})$  with  $\eta_c$  the cavity pump rate Following the solution of the ME (discussed below), the *steady-state* transmissivity and reflectivity are obtained:  $t \equiv |t|e^{i\phi_t} = \langle a_{out}^r \rangle_{ss} / \langle a_{in} \rangle$  and  $r \equiv |r|e^{i\phi_r} = \langle a_{out}^l \rangle_{ss} / \langle a_{in} \rangle$ , where  $\phi_t$  and  $\phi_r$  are the phases Working in a frame rotating with respect to the laser pump frequency,  $\omega_L$ , the model Hamiltonian can be written as

$$H = h\Delta_{xL}\sigma^+\sigma^- + h\Delta_{cL}a^+a + hg(\sigma^+a^- + a^+\sigma^-) + H_{drive}^c + \sigma^+\sigma^- \sum_q h\lambda_q(b_q + b_q^+) + \sum_q h\omega_q b_q^+ b_q, \tag{4}$$

where  $b_q$  ( $b_q^+$ ) are the annihilation and creation operators of the phonons,  $a$  is the cavity mode annihilation operator,  $\sigma^+$  and  $\sigma^-$  are the Pauli operators of the electron-hole pair

$$\frac{\partial p}{\partial t} = \frac{1}{i\hbar} [H_{sys}^+, p(t)] + L(p) + L_{ph}(p), \tag{5}$$

where the polaron -transformed system is Hamiltonian is

$$H'_{sus} = h(\Delta_{xL} - \Delta p)\sigma^+\sigma^- + h\Delta_{cL}a^+a + \langle B \rangle X_g + H_{drive}^c, \text{ with } \left[ -\frac{1}{2} \int_0^\infty d\omega J(\omega) / \omega^2 \coth(\beta\hbar\omega / 2) \right]$$

$$(\beta = 1/k_bT), X_g = hg(a^+\sigma^- + \sigma^+a), \text{ and } \Delta_p = \int_0^\infty d\omega J(\omega) / \omega.$$

Using a Markov approximation, the incompatible phononscattering term is defined as

$$L_{ph}(\rho) = \frac{1}{\hbar^2} \int_0^\infty d\tau \sum_{m=g,u} (G_m(\tau) \times [X_m e^{-iH_{sys}^+ \tau/\hbar} X_m e^{-iH_{sys}^+ \tau/\hbar} \rho(t)] + H.c.) \tag{6}$$

where  $x_u = -i\hbar g(a^+\sigma^- - \sigma^+a)$ , and  $g_{g/u}(t)$  are the polaron green functions:[25-30] Lindblad ME has been shown to yield very good agreement with the full polaron ME solution above. In this way, one defines the phonon-mediated incompatible scattering processes through

$$L_{ph}(\rho) = \frac{\Gamma_{ph}^{\sigma^+a}}{2} L(\sigma^+a) + \frac{\Gamma_{ph}^{\sigma^-a}}{2} L(a^+\sigma^-), \tag{7}$$

where  $G(D) = 2D\rho D^\dagger - D^\dagger D\rho - \rho D^\dagger D$ , and the scattering rates are obtained analytically,

$$\Gamma_{ph}^{\sigma^+ a / a^+ \sigma^-} = 2 \langle B \rangle^2 g^2 \operatorname{Re} \left[ \int_0^\infty d\tau e^{\pm i \Delta_{cx}} (e^{\phi(\tau)} - 1) \right], \dots\dots(8)$$

The rate  $\Gamma_{ph}^{\sigma^+ \sigma^-}$  describes the process of cavity excitation and the emission of exaction, via phonon-induced scattering..

## CONCLUSION

This paper presents the light propagation for QD- cavity geometry using Master equation.

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